

# Computer-Vision Jet Identification

Josh Cogan, Michael Kagan, **Emanuel Strauss**, Ariel Schwartzman



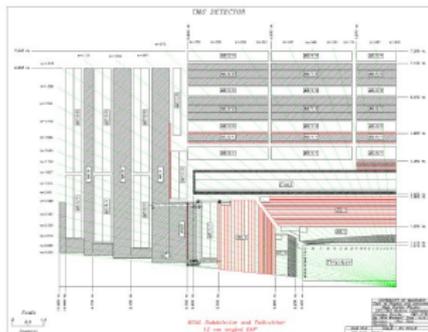
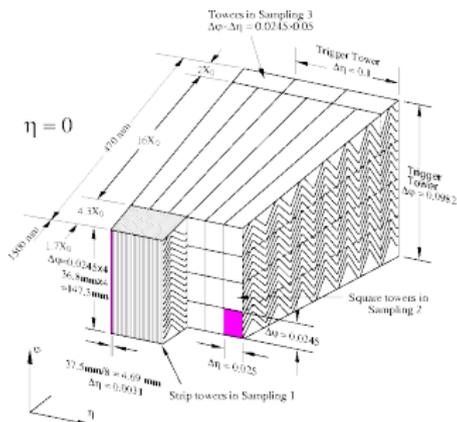
September 17, 2013

# Overview

1. Motivation of Boosted Searches
2. Overview of Classification Approaches
3. Jets as Images
4. Algorithm Overview
5. Case Study:  $W$  vs Light Jets
  - Image Processing
  - Applying the Discriminant
  - Cross-checks
6. Case Study:  $H \rightarrow b\bar{b}$  vs  $g \rightarrow b\bar{b}$
7. Case Study:  $q$  vs  $g$
8. Summary

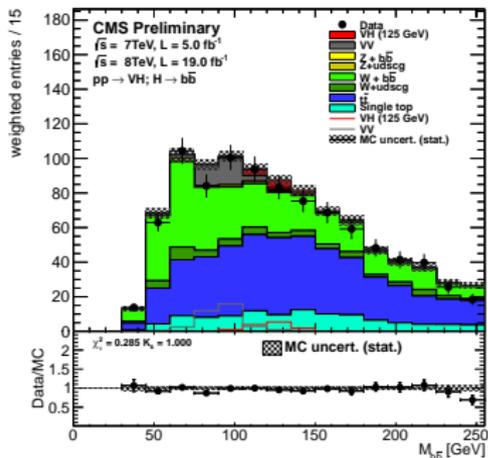
# Motivation of Boosted Searches

- ▶ Idea gained traction in 2008 by Butterworth, Davison, Rubin, and Salam as a way to recover  $V(H \rightarrow b\bar{b})$  channels.
  - Causes system to be more central (better tagging performance)
  - Additional background handles (additional jet activity)
- ▶ By consequence, overlapping signal jets:  $\Delta R_{b\bar{b}} \simeq \frac{1}{\sqrt{z(1-z)}} \frac{m_H}{p_T}$



- ▶ Fine segmentation of ATLAS and CMS calorimeters allows exploration of jet substructure.

# Boosted Objects at the LHC



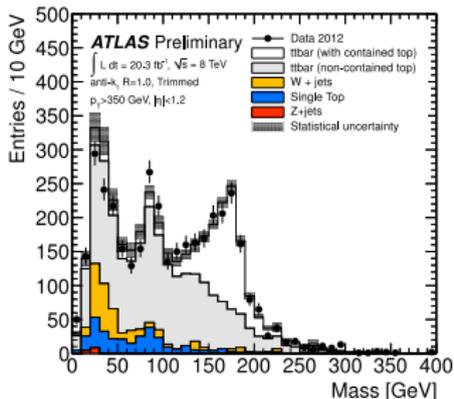
The future played out differently, but boost is a real part of LHC analyses:

- ▶ CMS (ATLAS)  $V(H \rightarrow b\bar{b})$ , three (five)  $V_{p_T}$  bins

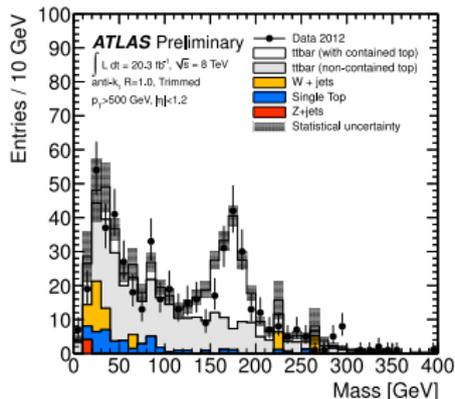
<http://arXiv.org/abs/0802.2470v2>

# Boosted Objects at the LHC

- ▶ ATLAS triggers on “Fat” jets with  $\Delta R = 0.1$
- ▶ **Boosted top** analyses have their best mass resolution in the high  $p_T$  bin.
  - All three decay products fully contained in a single jet
  - QCD  $p_T$  spectrum falls off rapidly



(a)  $p_T > 350$  GeV



(b)  $p_T > 500$  GeV

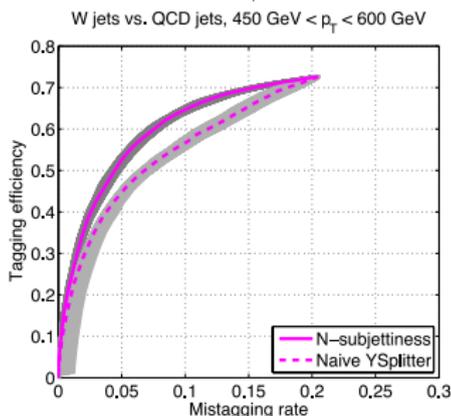
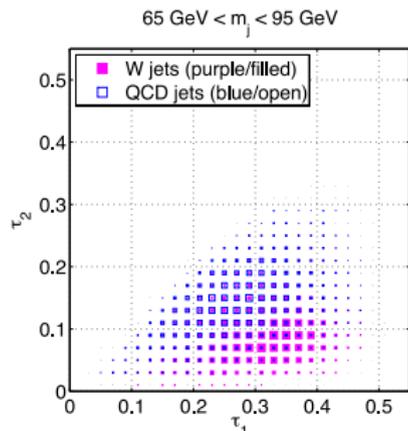
- ▶ MC Simulation does an admirable job of describing the data (due to immense amount of validation and performance work).

# Approaches to Substructure: N-Subjettiness

- ▶ Designed to identify boosted hadronically-decaying objects like EW bosons and top quarks.
  - Boosted bosons: 2 energetic, narrow, sub-jets.
  - QCD jets: several broader sub-jets.

$$\tau_N = \frac{1}{d_0} \sum_k p_{T,k} \min_A \Delta R_{A,k}$$

- $k$  – sum over jet constituents
  - $A$  – Minimize distance to candidate subjet axes
- ▶ W/Z/H tagging with  $\tau_2/\tau_1$ , top tagging with  $\tau_3/\tau_2$
  - ▶ “Intuitively” measures likelihood system is compatible with n-prong structure.

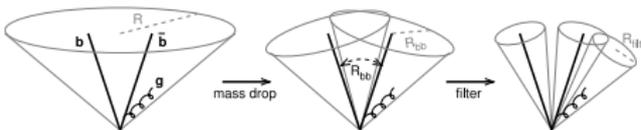


# Other Approaches

## Mass Drop

- ▶ Decompose the jet evolution.
- ▶ Given a hard jet, perform iterative decomposition.
  - Using Cambridge-Aachen jet clustering
- ▶ Find a subjets with  $m_{j1} < \mu m_{j2}$

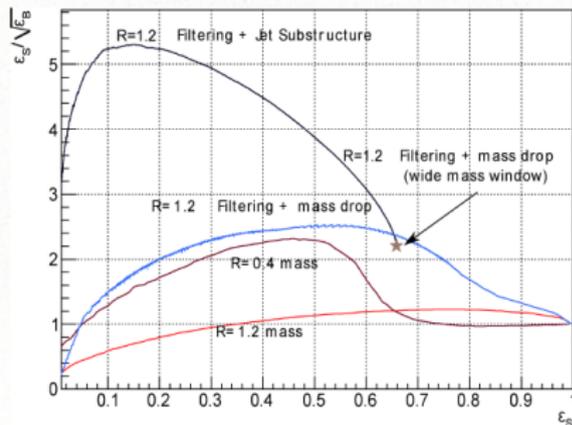
▶ And  $y = \frac{\min(p_{T1}, p_{T2})(\Delta R_{12})^2}{m_{\text{jet}}^2}$



- ▶ Originally proposed to improve  $H \rightarrow b\bar{b}$  selection.

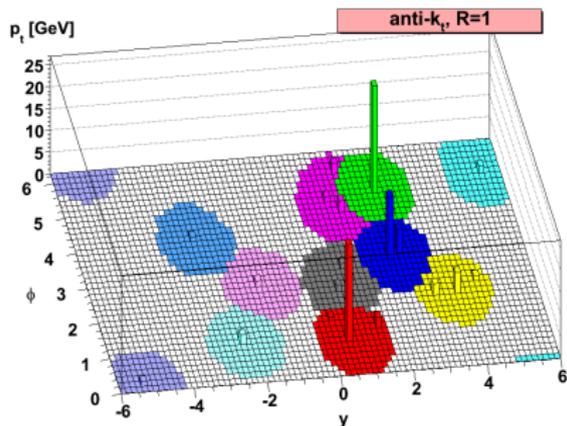
## MVA Tagger

- ▶ Attack the dimensionality problem.
- ▶ Many (well motivated) features describe a reconstructed jet.
- ▶ Use planar flow, jet shapes, etc. . .

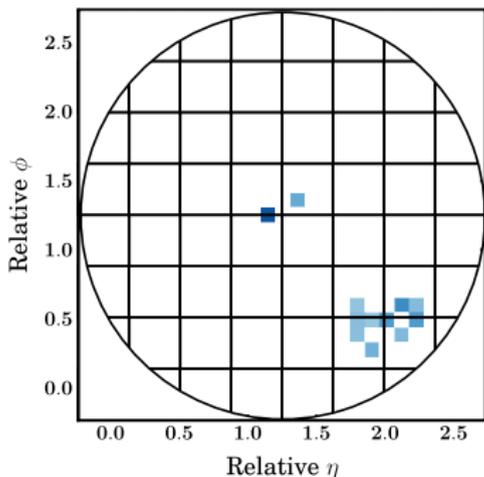


# Jets as Images

Most focus on a top-down approach (variables motivated by an analytical understanding of the problem), we tackle the problem from the bottom up.



Jet identification and sub-structure is generally treated as a form of cluster analysis.



Towers can just as easily be treated as the pixels of an image.

Uniform basis, with much lower dimensionality than machine vision (625 cells for  $\Delta\eta \times \phi = 0.1 \times 0.1$ , instead of  $\sim 1M$  for a picture)

# From Computer Vision To Jet Classification

Techniques for producing numerical values or decisions from high-dimensional data.

Mapping gender recognition onto jet identification:

- ▶ Face detection
  - Face region of interest finding
  - Eye detection
- ▶ Face preprocessing
  - Geometric transformation
  - Equalization
  - Noise reduction / smoothing
  - Masking
- ▶ Facial recognition / discrimination
  - Transformations
  - Training and using a discriminator
- ▶ Jet finding
  - Jet clustering
  - Grooming
  - Principal axis finding
- ▶ Jet preprocessing
  - Geometric transformation
  - Normalization
  - Masking
- ▶ Jet tagging / discrimination
  - Transformations
  - Training and using a discriminator

Demonstrate proof of principle using Monte Carlo with an idealized detector

# Practically Speaking

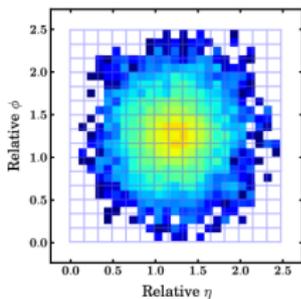
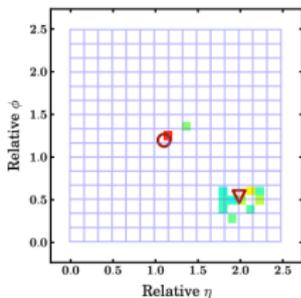
- ▶ Picking a representation
  - Considering only calorimeter towers (no track information)
  - Enforce a uniform representation by projecting the calorimeter energies onto a  $\Delta\eta \times \Delta\phi = 0.1 \times 0.1$  grid
  - Perform clustering (**Anti- $k_T$  with  $\Delta R = 1.2$** ) to find jets, apply **jet trimming** with radius 0.3 and  $f = 0.05$ .
  - Keep  $25 \times 25$  cells, centered around the jet.
  - Each jet is described by an uncurled row vector of cell energies (length = 625).
  
- ▶ Each jet is now **uniformly defined** by a single feature vector.
- ▶ Same number of variables per jet.
- ▶ Complete representation of the physics (within tower granularity).
- ▶ Set of feature vectors defines a **feature space**.
- ▶ Easily lends itself to feature extraction and dimensionality reduction.

# Case Study: $W$ vs Light Jets

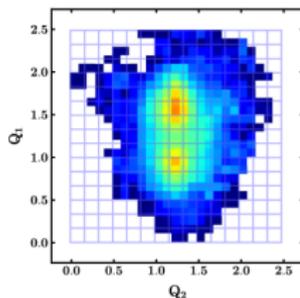
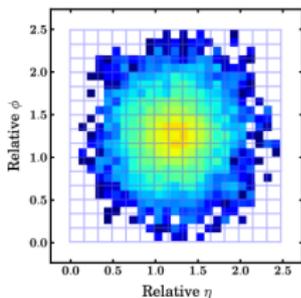
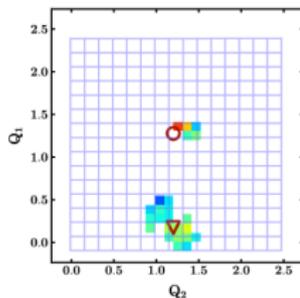
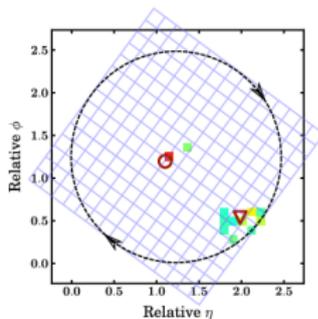
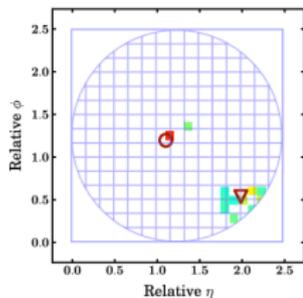
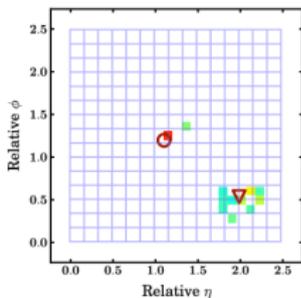
- ▶ Great system for algorithm development and validation
- ▶ Well known system with several attractive features:
  - $W$  decays to two quarks should be composed of **two distinct hard sub-jets**.
  - Decays have a fundamentally different **energy pattern** than QCD jets (for comparable jet masses).
  - Thoroughly explored in the literature (N-Subjettiness, MVA Tagger, etc. . . ).

If the method works here, it gives us good reason to try other systems as well.

# Image Processing

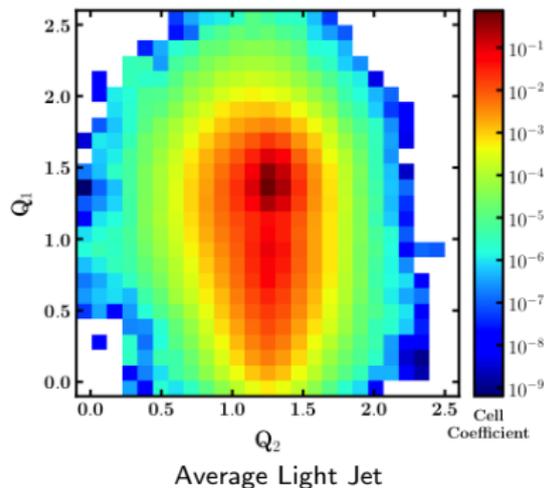
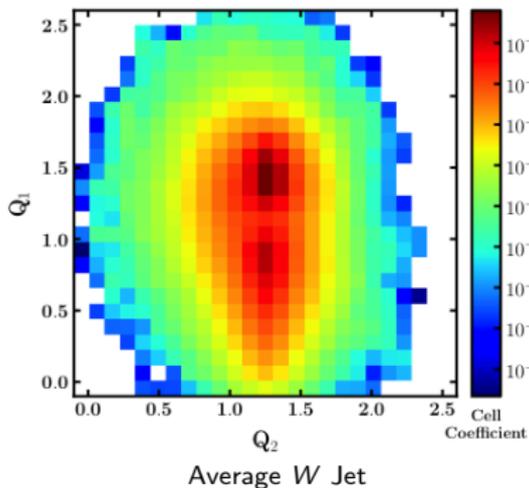


# Image Processing



# Building the Discriminant

Consistent “image” representation for calorimeter objects.

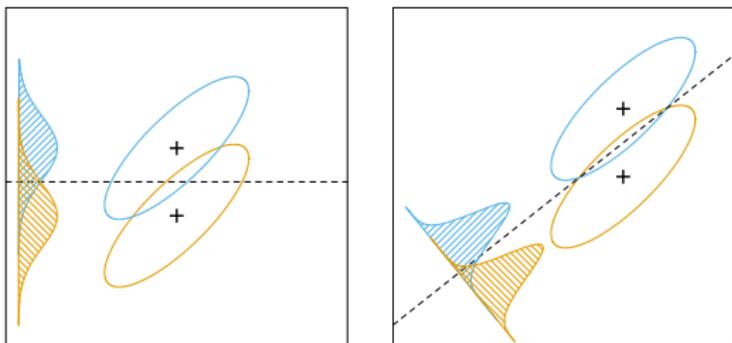


Now, turn this information into a number **we can cut on**.

# Fisher's Linear Discriminant

Finding a subspace which represents most of the **data variance**:

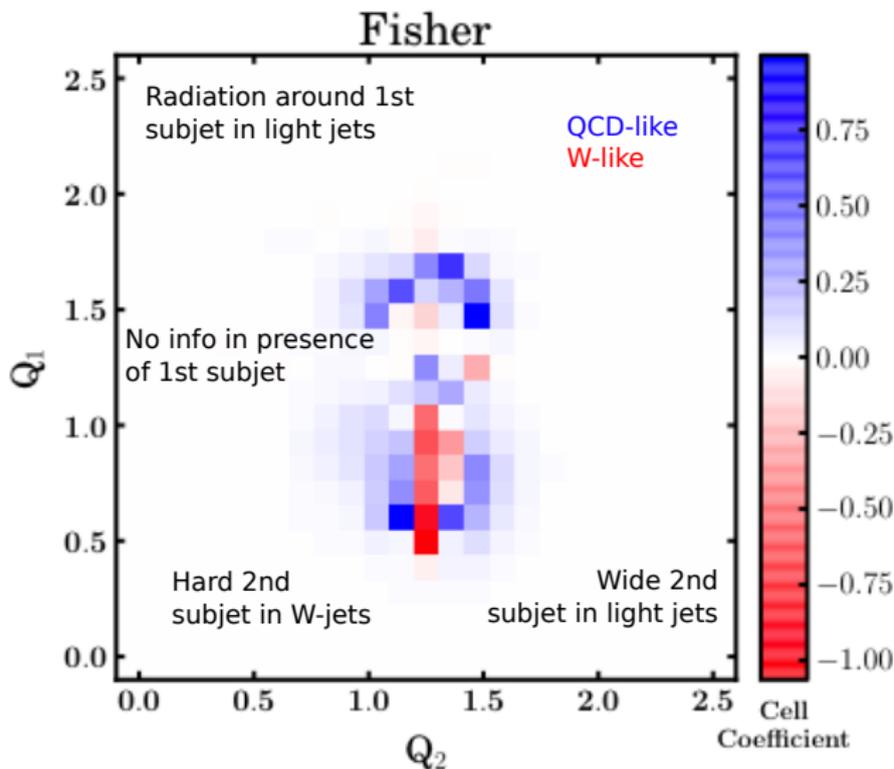
- ▶ Map same class sample vectors in a single spot of the feature representation.
  - Minimize **within class** differences:  $S_w = \sum_{i=1}^C \sum_{j=1}^N (x_j - \mu_i)(x_j - \mu_j)^T$
- ▶ Map those of different classes as far apart from each other as possible.
  - Maximize **between class** differences:  $S_b = \sum_{i=1}^C (\mu_i - \mu)(\mu_i - \mu)^T$



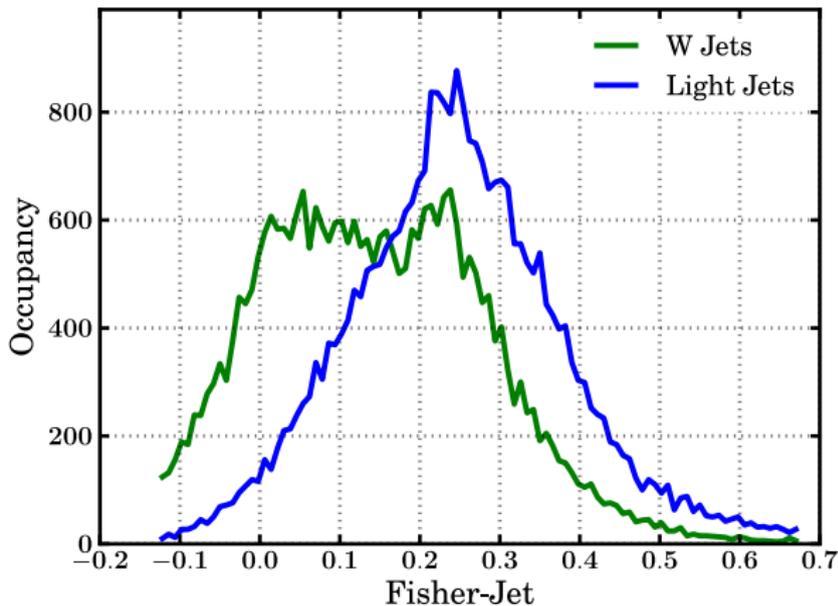
Find the basis vector  $V$  for:  $S_b V = (S_w + \sigma^2 I) V \lambda$

(Actually, even easier in the two class case.)

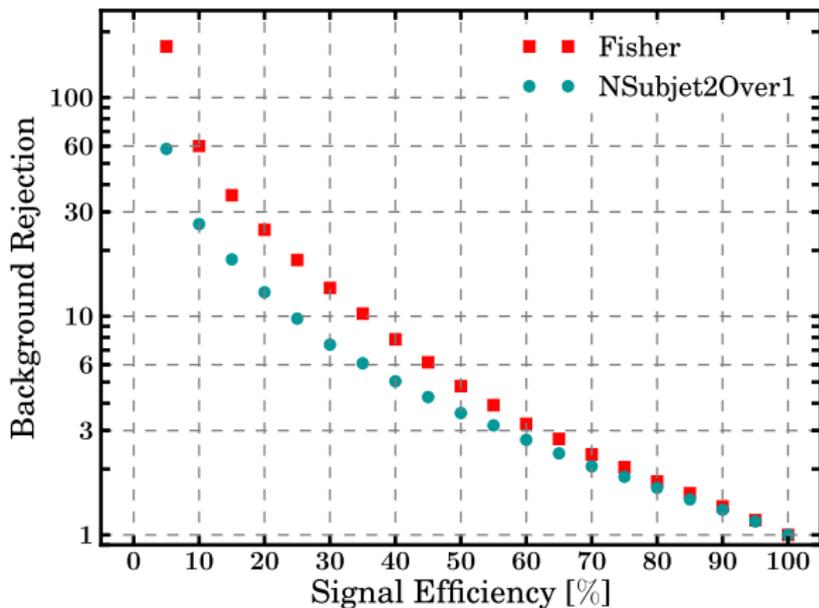
# Visualizing the Classifier



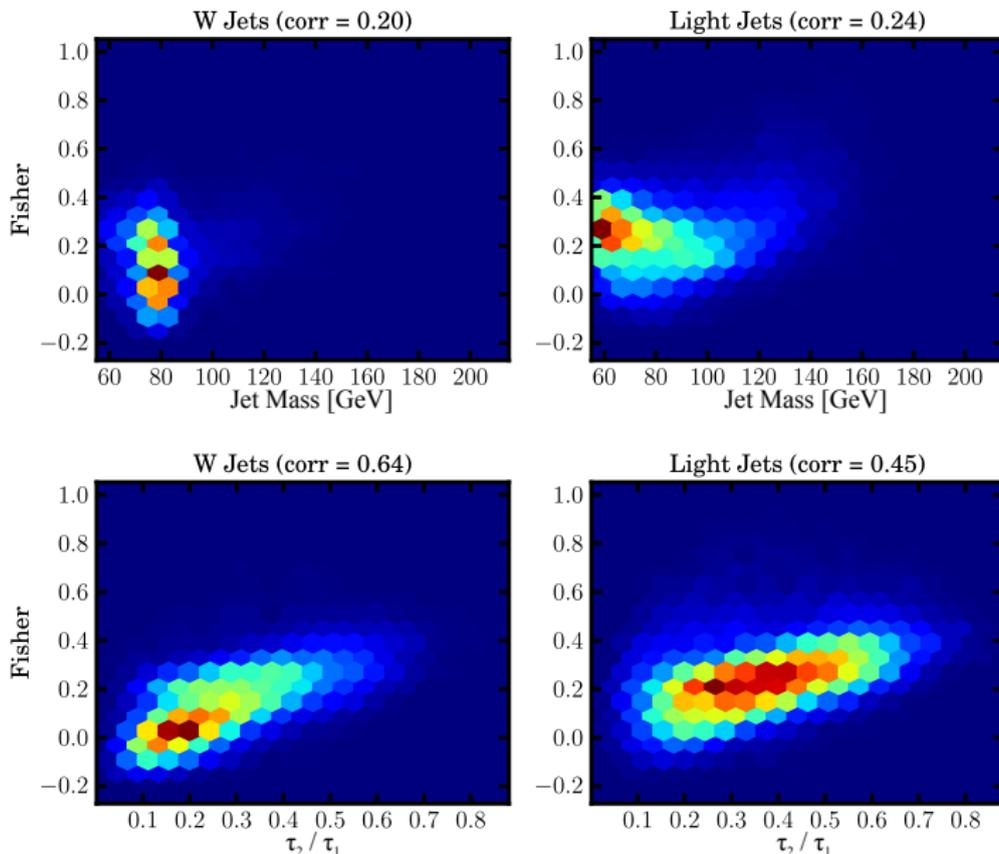
# Classifier Performance



# Classifier Performance



# Unique Information



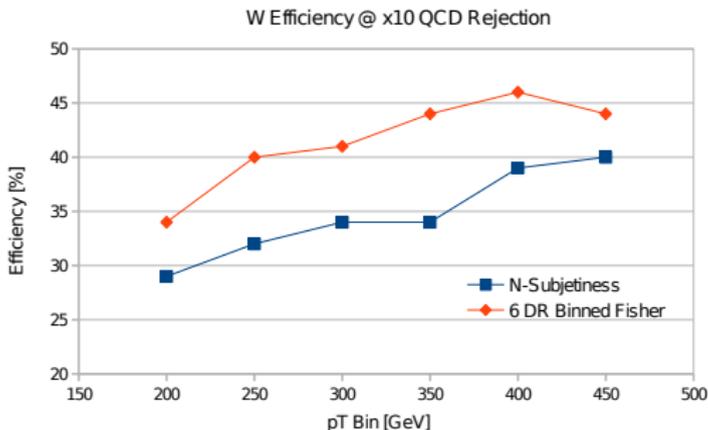
# Robustness

- ▶ Facial identification techniques are designed to perform well in the presence of deteriorated face images.
  - Gaussian noise
  - Salt and Pepper
  - Blurring
  - Partial Input
- ▶ A priori expect the method to work well based on the success in facial identification literature.

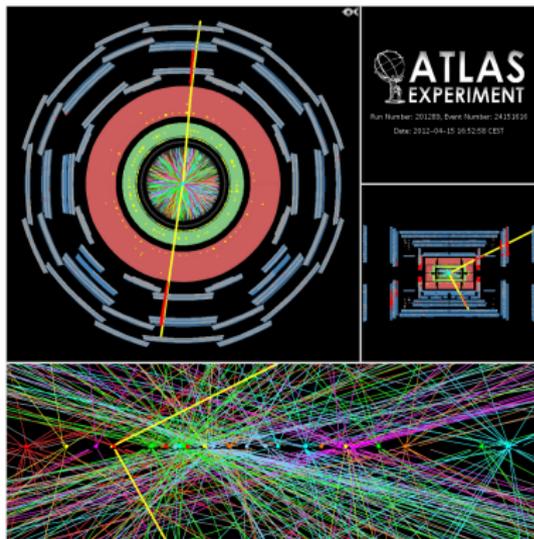


# $p_T$ Dependence

- ▶ Fisher discriminant is trained in 50 GeV bins
  - Improves the image “resolution”
  - Easier to generate MC to probe the full  $p_T$  spectrum
- ▶ Binning could be optimized, or extended into other variables.
- ▶ Performance is robust against jet  $p_T$



# Effects of Pileup

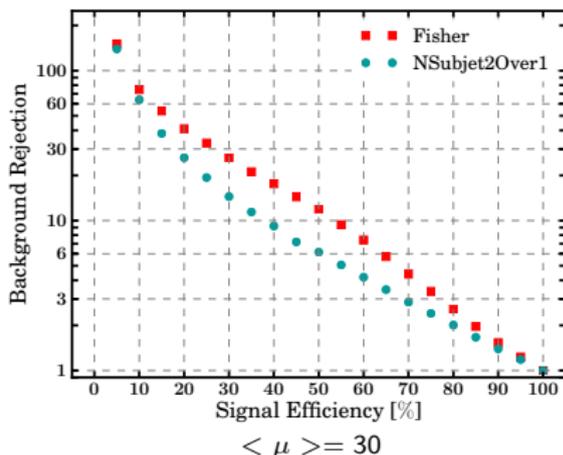
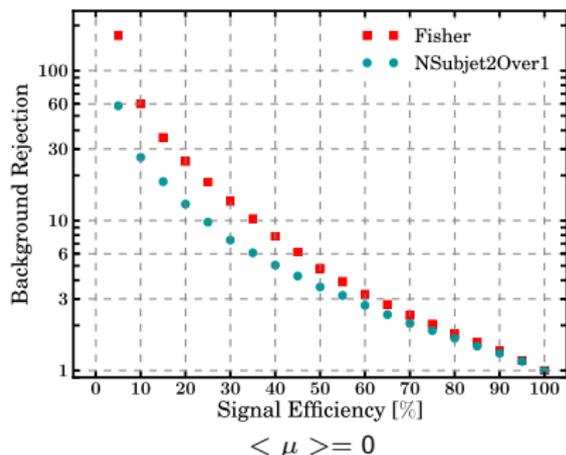


- ▶ One of the main challenges at the LHC
  - Additional interactions per bunch crossing (in-time)
  - Calorimeter integration time over multiple crossings (out-of-time)
- ▶ Additional event energy
- ▶ Increased fluctuations in the jet resolution noise term.
- ▶ Increased number of “fake” jets

# Pileup

Investigate effect of pileup by overlaying additional Pythia Minbias events.

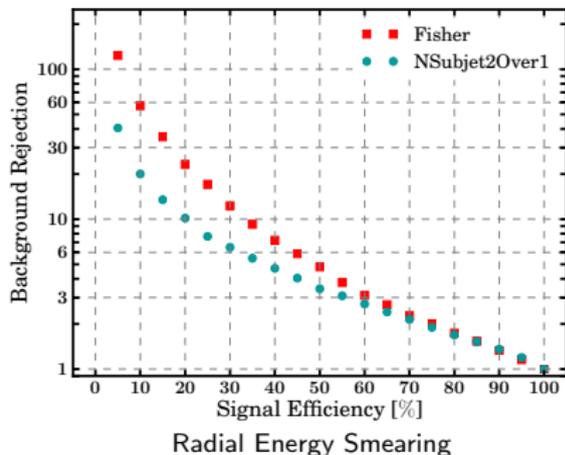
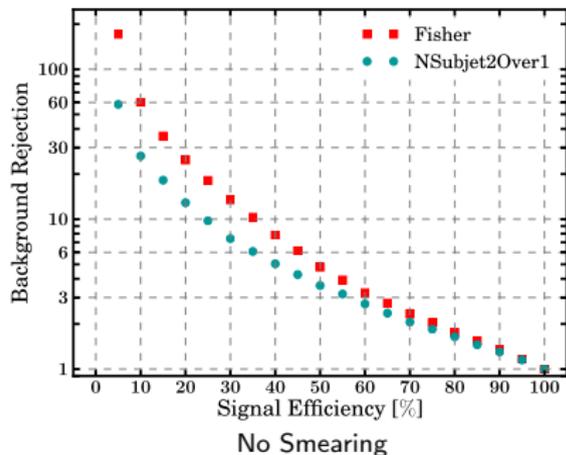
- ▶ Train on samples without pileup
- ▶ Test on W and L samples with  $\langle \mu \rangle = 0$  and 30.



- ▶ Note: statistically independent and differently distributed samples
  - Pre-selection for sig (bkg) increases by a factor of 1.5 (7).

# Radial Energy Smearing

- ▶ Simulate the energy spread introduced by **electromagnetic and hadronic showers** in calorimeters.
- ▶ Use an ATLAS-like setup with EM and HAD showers.

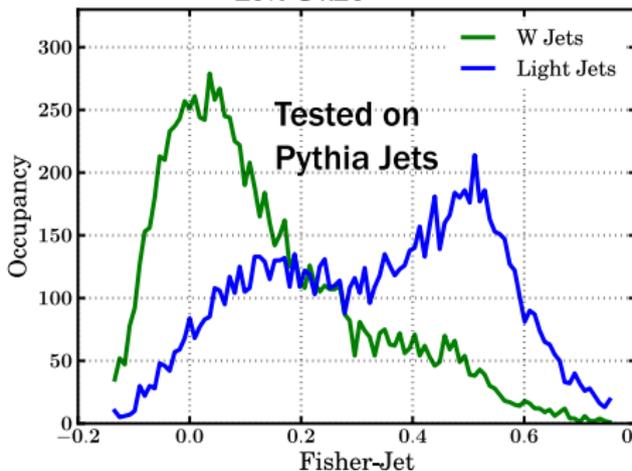


<http://atlas.physics.arizona.edu/~loch/>

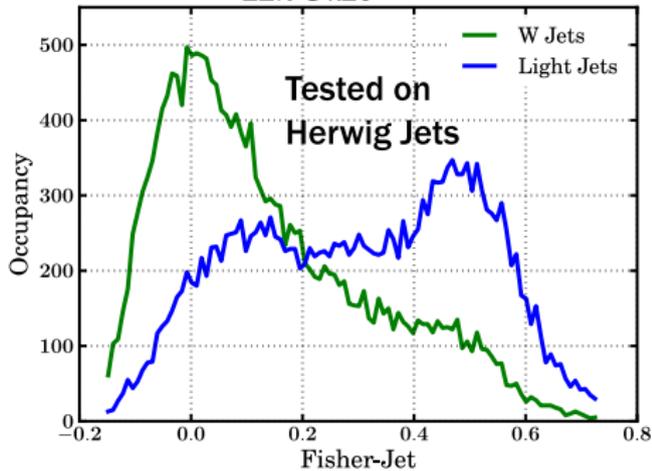
# Generator Model

- ▶ Check Pythia vs Herwig: want to see no sensitivity to differences
- ▶ Use the same discriminant (trained on Pythia jets)
- ▶ Similar performance when tested on Pythia or Herwig jets

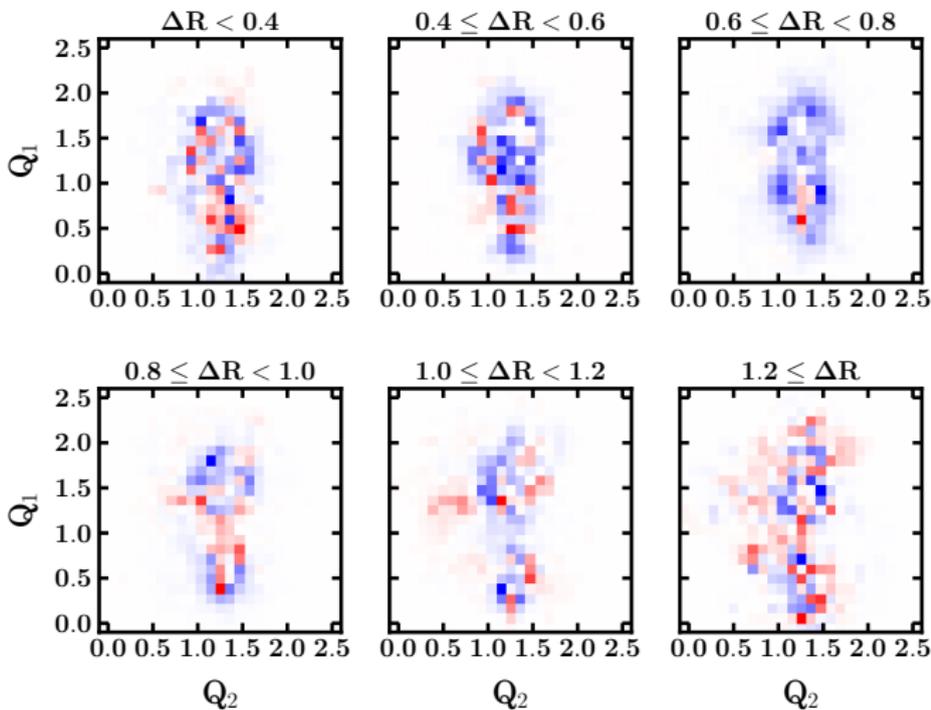
W eff @ QCD Rejection  
71% @ x2  
18% @ x10  
10% @ x20



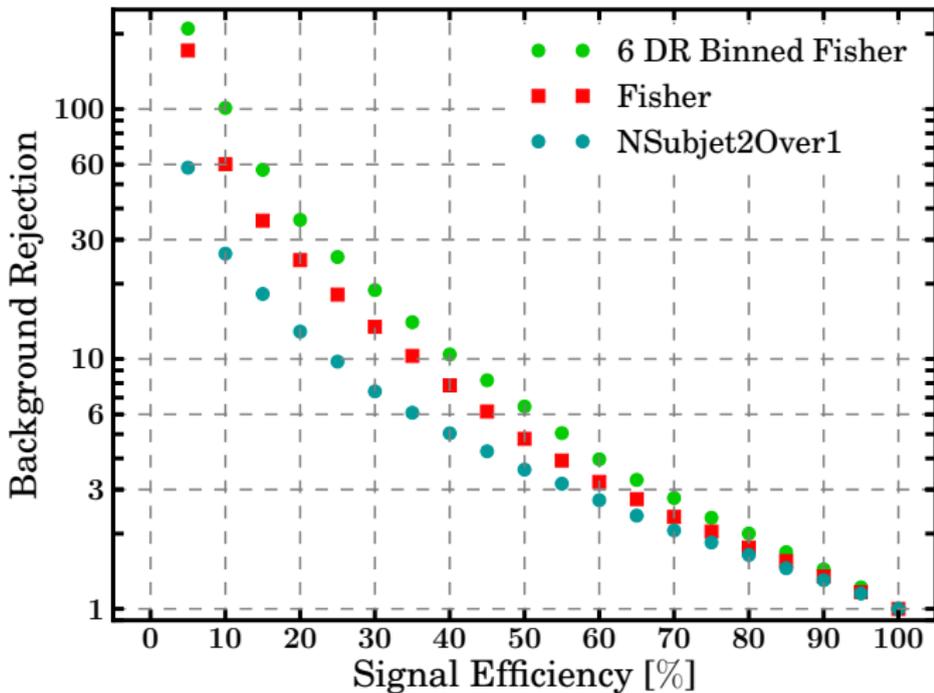
W eff @ QCD Rejection  
70% @ x2  
20% @ x10  
11% @ x20



# Binning The Classifier

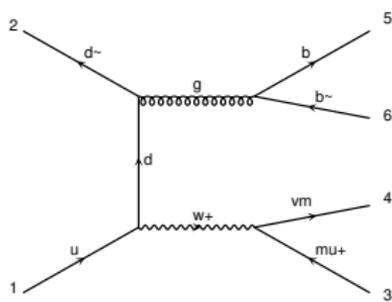
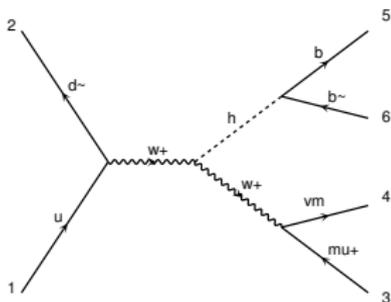


# Binning The Classifier



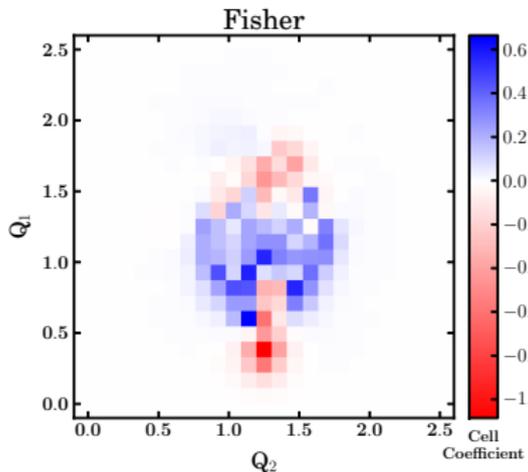
# Case Study: $H \rightarrow b\bar{b}$ vs $g \rightarrow b\bar{b}$

- ▶ The canonical example par excellence
  - Jet substructure looks very different, even if **mass**,  $p_T$ , etc. . . are the same.
- ▶ Potential for large boost in 14 TeV dataset.
  - Natural extension for moderately boosted analysis at 8 TeV

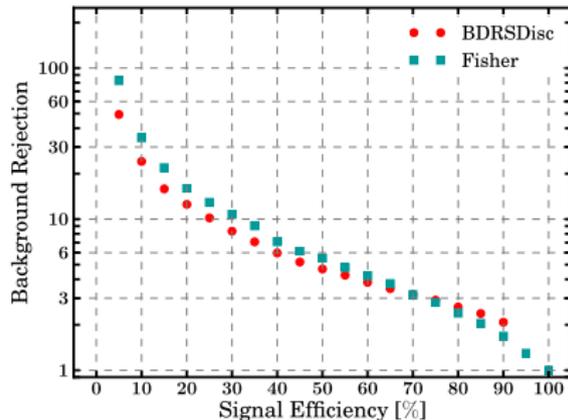


- ▶ Most powerful handle to date: *BDRS* corrected invariant jet mass
  - Potential to exploit additional b-tagging.

# Discriminant Performance



$300 < H_{p_T} < 350$  GeV,  $110 < m_{jj} < 125$  GeV,  
inclusive  $\Delta R$  classifier



- ▶ Performance is about the same **before and after** cuts on BDRS
- ▶ Can get x10 rejection for  $\sim 70\%$  acceptance using both.

# Case Study: $q$ vs $g$

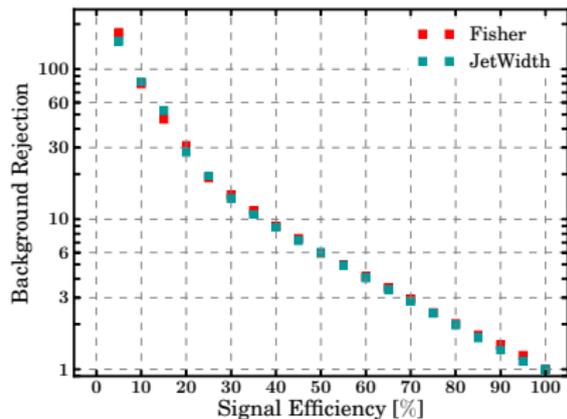
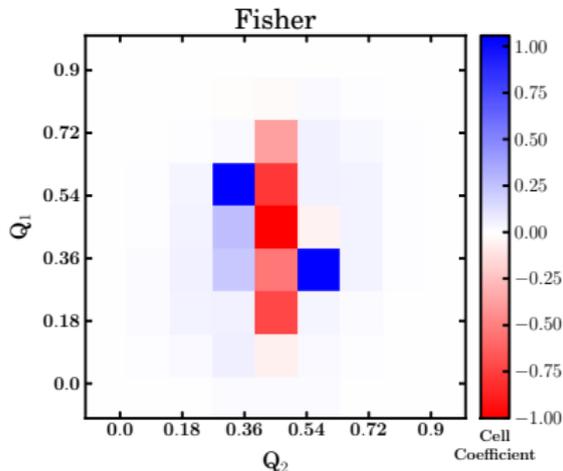
Most new physics is expected to produce quark jets, rather than gluon-initiated jets.

- ▶ SUSY cascade decays:  $\tilde{g} \rightarrow q\bar{q}\chi_1^0$
- ▶ Heavy  $Z' \rightarrow q\bar{q}$  or  $W' \rightarrow qq'$

And interesting SM physics tends also to produce quark-jets.

- ▶  $t\bar{t}$  to 4 or 6 quarks
- ▶ Vector Boson Fusion
- ▶ Boosted top, W, and Higgs!
  
- ▶ Switch from “fat” jets  $\Delta R = 1.2 \rightarrow 0.6$

# $q$ vs $g$ Performance



- ▶ Bottom-up approach performs identically to jet width.

# Wrap Up

- ▶ Generic method for calorimeter tagging using computer vision techniques
  - Many other systems to study: top vs light, particle ID (e.g. photon vs  $\phi^0$ ),  $b$ -tagging
  - Pileup detection and suppression
  - Most important conceptual step is the **image paradigm**, the rest is “simple”
- ▶ Provides a powerful tool for **gaining physics insight**
- ▶ In cases studied, performance is as good as, or better, than analytically motivated variables.
- ▶ Many parameters to vary in pre-processing
  - Normalization, center fixing, scaling, boosting, whitening
  - Alternative basis (e.g. cell  $p_T$  pairs, instead of cell  $p_T$ )
- ▶ Lots of room for extensions to the method
  - The contents of this talk covers up to the year  $\sim 2000$  in the literature
    - ★ Not limited to using linear classifiers in a two-class problem
  - Baseline method mature enough for **application to LHC analyses**
  - Documentation is being written up (expect it on the arxiv soon)

# Backup Slides

# Processing Time

- ▶ Method is extremely fast –  $\mathcal{O}(1ms)$  per jet

